Chapter 19 Confidence intervals: The basics

Types of Statistical Inference

- * Confidence intervals for estimating the value of a population parameter
- * Tests of significance assesses the evidence for a claim about a population.
 - Both types of inferences are based on the sampling distributions of statistics
 - ✓ Both report probabilities that state "what would happen if we used the inference method many times"
- When you use statistical inference, you are acting as if the data are a random sample or come from a randomized experiment.

Objectives

Confidence intervals: the basics

- > Estimating with confidence
- > Confidence intervals for the proportion or mean
- > How confidence intervals behave
- > Choosing the sample size

Estimating with confidence

Although the sample mean, $\overline{\chi}$, is a unique number for any particular sample, if you pick a different sample, you will probably get a different sample mean.

In fact, you could get many different values for the sample mean, and virtually none of them would actually equal the true population mean, $\mu.$



Statistical Inference

Statistical inference provides methods for drawing conclusions about a population from sample data.

What does _____% confidence really mean?

"In repeated samples of the same size, the confidence created will catch the true value/parameter (p) _____ of the time."

In repeated samples of size 30, the conf. interval created will catch the true winning percent of the GAME 95% of the time.

We are 95% confident that the true % of chickens infected with Salmonella is between 11.95% and 18.05%.

What does _____ % confidence really mean? Whenever we create a confidence interval, we write a sentence interpretation:

"Based on our sample, we are 95% confident that the <u>true % (or proportion)</u> of (<u>content)</u> is between <u>a</u> and <u>b</u> %.

Example: President Obama 45% approval rating, MOE of 3%, 95% confidence:

We are 95% confident that the true % approval rating of President Obama is between 42% and 48%.









Confidence Level Z* 90% 0.1. Summarize your results in a simple table Confidence Level Z* 90% 1.645 95% 1.960 99% 2.576

≻ N(0, 1)

> Use invNorm(*p*, 0, 1)























Sample size and experimental design

You may need a certain margin of error (e.g., drug trial, manufacturing specs). In many cases, the population variability (s) is fixed, but we can choose the number of measurements (*n*).

So plan ahead what sample size to use to achieve that margin of error.

$$m = z * \frac{\sigma}{\sqrt{n}} \quad \Leftrightarrow \quad n = \left(\frac{z * \sigma}{m}\right)^2$$

Remember, though, that sample size is not always stretchable at will. There are typically costs and constraints associated with large samples. The best approach is to use the smallest sample size that can give you useful results.





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