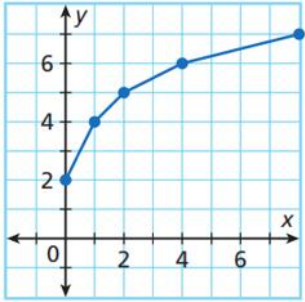


## 7.2: INVERSES OF RELATIONS AND FUNCTIONS

- To graph the inverse relation, reflect each point across the line  $y = x$ . This is equivalent to switching the  $x$ - and  $y$ -values in each ordered pair of the relation.

### Example 1: Graphing Inverse Relations

Graph the relation and connect the points. Then graph the inverse. Identify the domain and range of each relation.



$x$	0	1	2	4	8
$y$	2	4	5	6	7

	Domain	Range
$f(x)$		
$f^{-1}(x)$		

### HOW TO FIND THE INVERSE OF A RELATION

- Given  $f(x)$ . Rewrite it as  $y$ , then switch  $x$  and  $y$ .
- Solve for  $y$ .
- Rewrite the computed  $y$  as  $f^{-1}(x)$ .

**Example 2:** Use inverse operations to write the inverse of each function. Then identify the domain and range.

a)  $f(x) = 3x + 4$

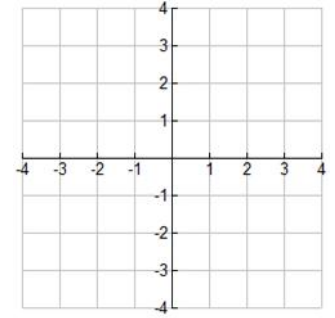
b)  $g(x) = x^2 - 6x + 9$

c)  $f(x) = \frac{1}{2}(4 - 3x)$

d)  $g(x) = 3\sqrt{x+5} - 4$

**Example 3:** Find the inverse of the function then write and graph the function and its inverse.

a)  $f(x) = 3x - 2$



**Example 4:** The A clerk needs to price a digital camera returned by a customer. The customer paid a total of \$103.14, which included a gift-wrapping charge of \$3 and 8% sales tax. What price should the clerk mark on the tag?

**Example 5:** The formula  $C = \frac{5}{9}(F - 32)$  gives degrees Celsius as a function of degrees Fahrenheit. Find the inverse of this function to convert degrees Celsius to Fahrenheit and use it to find  $16^\circ\text{C}$  in degrees Fahrenheit.

**Example 6:** Eliza's auto repair bill includes \$175 for parts and \$35 per hour for labor. The bill can be expressed as a function of hours  $x$  with the function  $f(x) = 175 + 35x$ . Which statement explains the meaning of the inverse of the function?

- (F) Number of hours as a function of the total bill
- (G) Total bill as a function of the number of hours
- (H) Cost per hour as a function of the total bill
- (J) Total bill as a function of the cost per hour