



Objectives

Producing data: sampling

- * Observation versus experiment
- * Population versus sample
- * Sampling methods
- Simple random samples
- Stratified samples
- Caution about sampling surveys
- * Learning about populations from samples

Background

- We have learned ways to display, describe, and summarize data, but have been limited to examining the particular batch of data we have.
- To make decisions, we need to go beyond the data at hand and to the world at large.
- Let's investigate three major ideas that will allow us to make this stretch...

3 Key Ideas That Enable Us to Make the Stretch



We settle for examining a smaller group of individuals—a sample—selected from the population.

Idea 1: Examine a Part of the Whole

Examples:

- Sampling is a natural thing to do. Think about sampling something you are cooking—you taste (examine) a small part of what you're cooking to get an idea about the dish as a whole.
- Opinion polls are examples of sample surveys, designed to ask questions of a small group of people in the hope of learning something about the entire population.
 - Professional pollsters work quite hard to ensure that the sample they take is representative of the population.
 - If not, the sample can give misleading information about the population.





Bias

- Sampling methods that, by their nature, tend to overor under- emphasize some characteristics of the population are said to be **biased**.
 - Bias is the bane of sampling—the one thing above all to avoid.
 - There is usually no way to fix a biased sample and no way to salvage useful information from it.
- The best way to avoid bias is to select individuals for the sample at random.
 - The value of deliberately introducing randomness is one of the great insights of Statistics.

Idea 2: Randomize

- **Randomization** can protect you against factors that you know are in the data.
 - It can also help protect against factors you are not even aware of.
- Randomizing protects us from the influences of all the features of our population, even ones that we may not have thought about.
 - Randomizing makes sure that on the average the sample looks like the rest of the population.

Randomizing (cont.)

- Not only does randomizing protect us from bias, it actually makes it possible for us to draw inferences about the population when we see only a sample.
- Such inferences are among the most powerful things we can do with Statistics.
- **But** remember, it's all made possible because we deliberately choose things randomly.



Idea 3: It's the Sample Size

- How large a random sample do we need for the sample to be reasonably representative of the population?
- It's the size of the sample, not the size of the population, that makes the difference in sampling.
 - Exception: If the population is small enough and the sample is more than 10% of the whole population, the population size *can* matter.
- The fraction of the population that you've sampled doesn't matter. It's the sample size itself that's important.

Example:

- i) In the city of Chicago, Illinois, 1,000 likely voters are randomly selected and asked who they are going to vote for in the Chicago mayoral race.
- ii) In the state of Illinois, 1,000 likely voters are randomly selected and asked who they are going to vote for in the Illinois governor's race.
- iii) In the United States, 1,000 likely voters are randomly selected and asked who they are going to vote for in the presidential election.
- Which survey has more accuracy?
 - All the surveys have the same accuracy

Observation vs. experiment

Observational study: Record data on individuals without attempting to influence the responses. We typically cannot prove anything this way.

Example: Based on observations you make in nature, you suspect that female crickets choose their mates on the basis of their health. → Observe health of male crickets that mated.



Experimental study: Deliberately impose a treatment on individuals and record their responses. Influential factors can be controlled.



Example: Deliberately infect some males with intestinal parasites and see whether females tend to choose healthy rather than ill males.

Does a Census Make Sense?

- Why bother worrying the sample size?
- Wouldn't it be better to just include everyone and "sample" the entire population?
 - Such a special sample is called a census.

Does a Census Make Sense?

- There are problems with taking a census:
 - <u>Practicality</u>: It can be difficult to complete a census there always seem to be some individuals who are hard to locate or hard to measure.
 - <u>Timeliness</u>: populations rarely stand still. Even if you could take a census, the population changes while you work, so it's never possible to get a perfect measure.
 - <u>Expense</u>: taking a census may be more complex than sampling.
 - <u>Accuracy</u>: a census may not be as accurate as a good sample due to data entry error, inaccurate (made-up?) data, tedium.





Census vs. Survey

- A census is a study in which every member of a population provides information of interest.
- A survey is a study in which a sample of a population provides information of interest.

Sample Statistics Estimate Parameters

- Values of **population** parameters are unknown; in addition, they are <u>unknowable.</u>
- *Example:* The distribution of heights of adult females (at least 18 yrs of age) in the United States is approximately symmetric and mound-shaped with mean μ. μ is a population parameter whose value is unknown and <u>unknowable</u>
- * The heights of 1,500 females are obtained from a sample of government records. The sample mean \overline{x} of the 1,500 heights is calculated to be 64.5 inches.
- \diamond The sample mean \overline{x} is a sample statistic that we use to estimate the unknown population parameter μ

We typically use Greek letters to denote parameters and Latin letters to denote statistics.

Name	Statistic	Parameter	
Mean		μ (mu)	
Standard deviation	5	σ (sigma)	
Correlation	r	ρ (rho)	
Regression coefficient	b	β (beta)	
Proportion	p	p	















Response Bias

refers to anything in the survey design that influences the responses.

- Interviewer bias
- Untruthful responses
- The wording of a question

Work hard to avoid influencing responses!



bias equal error

- Sampling error is just sampling variation.
- Sampling error simply describes the natural variability in results that will be observed from one sample to the next, none of them exactly capturing the truth in the population.

Bias (ugh!) found in the sampling method..... Something about the design *systematically distorts the results* so that they are unlikely to reflect reality.





more response bias...

Other examples:

•A uniformed campus police office visits your class and asks every student about their drug use in the last 30 days...

•Your boss at work announces that they need to trim the workforce (read: they need to fire some people), then interviews and asks every employee:

"Are you satisfied with your current job at this company?"

Bias through wording of a question

• Be careful in phrasing answers. It is often a good idea to offer choices rather than inviting a free response. Open-ended answers can be difficult to analyze. Be sure to phrase them in a neutral way.

Subtle differences in phrasing can make a big difference

In January 2006, the *New York Times* asked half of the 1229 U.S. adults in their sample the following question:

After 9/11, President Bush authorized government wiretaps on some phone calls in the U.S. without getting court warrants, saying this was necessary to reduce the threat of terrorism. Do you approve or disapprove of this?

53% of respondents approved.

ubtle differences in phrasing can make a big difference!

...but when they asked the other half of their sample a question with only slightly different wording:

After 9/11, George W. Bush authorized government wiretaps on some phone calls in the U.S. without getting court warrants. Do you approve or disapprove of this?

... only 46% approved

le differences in phrasing can make a big difference!

- a) After 9/11, President Bush authorized government wiretaps on some phone calls in the U.S. without getting court warrants, saying this was necessary to reduce the threat of terrorism. Do you approve or disapprove of this?
- b) After 9/11, George W. Bush authorized government wiretaps on some phone calls in the U.S. without getting court warrants. Do you approve or disapprove of this?

Bias through wording of question

- Spring, 1993, Holocaust Memorial Museum opened in Washington, DC.
- Survey conducted by Roper Starch Worldwide indicated that 22 percent of the American public believed it "possible that the Nazi extermination of the Jews never happened", while another 12 percent were unsure.
- Exact wording of the **Roper** question:

Does it seem possible, or does it seem impossible to you that the Nazi extermination of the Jews never happened?

- Gallup question in a new poll: Does it seem possible to you that the Nazi extermination of the Jews never happened, or do you feel certain that it happened?
- less than 1% responded that they thought it was possible it did not happen

Source of Bias?

1) Before the presidential election of 1936, FDR against Republican ALF Landon, the magazine *Literary Digest* predicting Landon winning the election in a 3-to-2 victory. A survey of 2.8 million people George Gallup surveyed only

Undercoverage – since the Digest's survey comes from car owners, etc., the people selected were mostly from high-income families and thus mostly Republican! (other answers are possible)

2) Suppose that you want to estimate the total amount of money spent by students on textbooks each semester at

Convenience sampling – easy way to collect data

Undercoverage – students who buy books from on-line bookstores are not included.

Example: Hospital employee drug use

- Name the kind of bias that might be present if the administration decides that instead of subjecting people to random testing they'll just...
 - a) interview employees about possible drug abuse.
 - Response bias: people will feel threatened, won't answer truthfully
 - b) ask people to volunteer to be tested.
 - Voluntary response bias: only those who are "clean" would volunteer

Example: Hospital employee drug use

Listed in the table are the names of the 20 pharmacists on the hospital staff. Use the random numbers listed below to select three of them to be in the sample.

00 Pastore	10 Back
01 Spiridinov	11 Ahl
02 Hedge	12 MacDowell
03Schissel	13 Novelli
04 Lavine	14 Kaplan
05 Highland	15 Roundy
06 Grubb	16 Markowitz
07 Glass	17 Davies
08 Golkowski	18 Reeves
09 Janis	19 Yen

■ 04905 83852 29350 91397 19994 65142 05087 11232

Simple random samples (SRS)

- *Technically speaking:* Choose a set of *n* individuals from a population in a manner such that *all sets of size n* had an equal chance of being chosen.
- Samples drawn at random generally differ from one another.
 Each draw of random numbers selects *different* people for our sample.
 - These differences lead to different values for the variables we measure.
 - We call these sample-to-sample differences sampling variability.

Simple random samples (SRS)

The **simple random sample (SRS)** is made of randomly selected individuals. Each individual in the population has the same probability of being in the sample and no individual chooses to include/exclude a member of the population. All

possible samples of size \boldsymbol{n} have the same chance of being drawn.

- To select a sample at random, we first need to define where the sample will come from.
 - The **sampling frame** is a list of individuals from which the sample is drawn.
- Once we have our sampling frame, the easiest way to choose an SRS is to assign a random number to each individual in the sampling frame.

Simple Random Sample

- Advantages
 Disadvantages
 - -Unbiased -Large variance
 - -Easy
- May not be representative
- Must have sampling frame (list of population)



Cho	osing	a Sirr	ple F	Rando	om Sa	ample	
□ From size :	n a popul 5 using th	ation of is table	25 indiv	viduals,	choose	an SRS of	Ĩ
	19223	95034	05752	28713	06409	12531	
19: c	hoose						
22: c	hoose						
39: ig	nore (there	is not a p	erson nun	nber 39)			
50: ig	nore						
34: ig	nore						
05: c	hoose						
75: ig	nore						
22: ig	nore (perso	on number	22 is alre	ady in the	e SRS)		
87: ig	nore						
13: c	hoose						
06: c	hoose						

Choosing a Simple Random Sample

We need to select a random sample of 5 from a class of 20 students.

- 1) List and number all members of the population, which is the class of 20.
- 2) The number 20 is two-digits long.
- Parse the list of random digits into numbers that are two digits long. Here we chose to start with line 103, for no particular reason.

TABLE B Random digits

01	19223	95034	05756	28713	95409	12531	42544	82853
102	73676	47150	99400	01927	27754	42648	82425	36290
103	45467	71709	77558	00095	32863	29485	82226	90056
104	52711	38889	93074	60227	40011	85848	48767	52573
105	95592	94007	69971	91481	60779	53791	17297	59335
106	68417	35013	15529	72765	85089	57067	50211	47487
107	82730	57890	20807	47511	81676	55300	94383	14893





Systematic Random Samples

Suppose we want a sample of 5 students from this class of 35.

- $\ensuremath{\,\square}$ Then we need 5 equal-sized groups.
- So there are 7 members of each group
 Use the table of random numbers to choose the first
- member of the sample.
 - Go to any line in the table and find the first digit that is in the 1 7 range
- For example, using line 129 gives 3
- Then that same position in the group is used in all other groups
 - So the sample consists of persons numbered 3, 10, 17, 24, and 31
 - Note that we just add group size to each number to get the next number

Systematic Random Sample

Advantages Disadvantages

- Unbiased
- Don't need sampling frame
- Ensure that the
 - sample is spread across – population
- confounded by trend or cycle - Formulas are

-Large variance

-Canbe

- ation complicated
- More efficient, cheaper, etc.

Stratified Random Samples

- Sometimes we want to be sure that different types of individuals are included in the sample
 - Different gender, age, political party, race, geographical region, etc.
- The population is first divided into two or more strata (naturally occurring groups of similar individuals)
- Separate SRS's are chosen from each stratum, then combined to form the full sample

Stratified Random Samples

For example:

- Divide the population of UC-Berkeley students into males and females.
- Divide the population of California by major ethnic group.
- Divide the counties in America as either urban or rural based on a criterion of population density.

The SRS taken within each group in a stratified random sample need not be of the same size.

For example:

- Stratified random sample of 100 male and 150 female UC-B students
- Stratified random sample of a total of 100 Californians, representing proportionately the major ethnic groups

Stratified

Advantages Disadvantages

- More precise unbiased estimator than SRS
- Difficult to do if you must divide stratum
- Less variability
- Cost reduced
 - if strata mor already exists - Nee
- intervals are more complicated - Need sampling

- Formulas for SD

& confidence

frame

- Multistage Samples
 Suppose we want to sample a very large population such as all residents of the U.S.
- It is not practical to number them all and choose an SRS
- Instead, list (and number) some workable sub-group, such as all counties in the U.S.
 - □ There are about 3000 counties large but workable!
 - Take an SRS to choose which counties are included
- Within each county, list and number all communities
 Take an SRS to choose which communities are included
- Within each chosen community, list and number a subdivision such as residential blocks or Census Tract
 Take an SRS to choose which blocks are included
- Take an SRS of the households in the chosen blocks to form the actual sample

 Multistage samples
 use multiple stages of stratification. They are often used by the government to obtain information about the U.S. population.

 Example:
 Sampling both urban and rural areas, people in different ethnic and income groups within the urban and rural areas, and then

ethnic and income groups within the urban and rural areas, and then individuals of different ethnicities within those strata.

Data are obtained by taking an SRS for each substrata

Statistical analysis for multistage samples is more complex than for an SRS.







women. This problem is slowly being recognized

 To assess the opinions of students at the Ohio State University regarding campus safety, a reporter interviews 15 students he meets walking on the campus late at night who are willing to give their opinions.

- \rightarrow What is the sample here? What is the population? Why?
- All those students walking on campus late at night
- All students at universities with safety issues
- The 15 students interviewed
- All students approached by the reporter

2) An SRS of 1200 adult Americans is selected and asked: "In light of the huge national deficit, should the government at this time spend additional money to establish a national system of health insurance?" Thirty-nine percent of those responding answered yes.

- \rightarrow What can you say about this survey?
- The sampling process is sound, but the wording is biased. The results probably understate the percentage of people who do favor a system of national health insurance.

Should you trust the results of the first survey? Of the second? Why?

Cluster Sampling

and addressed.

- Sometimes stratifying isn't practical and simple random sampling is difficult.
- Splitting the population into similar parts or clusters can make sampling more practical.
- Then we could select one or a few clusters at random and perform a census within each cluster. This compliant design is called cluster compliant.
- This sampling design is called cluster sampling.
- If each cluster fairly represents the full population, cluster sampling will give us an unbiased sample.



Mean length of sentences in our course text



reading level of our course text based on the length of the sentences

· We would like to assess the

- Simple random sampling would be awkward:
 number each sentence in the book?
- <u>Better way</u>:

needed)

- choose a few pages at random (the pages are the clusters, and it's reasonable to assume that each page is representative of the entire text).
- · count the length of the sentences on those pages



Cluster Samples Advantages - Unbiased - Cost is reduced - Sampling frame may not be available (not - Clusters may not be available (not - Clusters may not be complicated

Learning about populations from samples

The techniques of inferential statistics allow us to draw inferences or conclusions about a population from a sample.

- Your estimate of the population is only as good as your sampling design \rightarrow Work hard to eliminate biases.
- Your sample is only an estimate—and if you randomly sampled again, you would probably get a somewhat different result.
- The bigger the sample the better. We'll get back to it in later chapters.





Identify the sampling design

1)The Educational Testing Service (ETS) needed a sample of colleges. ETS first divided all colleges into groups of similar types (small public, small private, etc). Then they randomly selected 3 colleges from each group.

Stratified random sample

Identify the sampling design

 A county commissioner wants to survey people in her district to determine their opinions on a particular law up for adoption. She decides to randomly select blocks in her district and then survey all who live on those blocks.

Cluster sampling

Identify the sampling design

3) A local restaurant manager wants to survey customers about the service they receive. Each night the manager randomly chooses a number between 1 & 10. He then gives a survey to that customer, and to every 10th customer after them, to fill it out before they leave.

Systematic random sampling

A research group wishes to know the mean GPA of all 2544 students at XYZ High School. To estimate this, they take a random sample of 189 students that have zone classes in the C-wing, and pull those records. The mean GPA of the students in the sample is 2.98. According to the school registrar, the GPA of all 2544 students at XYZ is 3.09.

Identify the following

a)Population (of interest): all XYZ HS students

b)Parameter of interest: mean GPA of all students

c)Sampling frame: just students with zone in C-wing

d)Sample: the 189 students selected

A neighborhood interest group wants to know what proportion of households in Austin watch the TV show "So You Think You Can Dance." They select a random sample of 59 houses from Northwest Austin, and find that 35.6% of those families watch the program regularly. Local ratings indicate that about 22% of all households watch SYTYCD on a regular basis.

Identify the following

- a) Population (of interest): households in Austin
- b) Parameter of interest: proportion of households that watch SYTYCD
- c) Sampling frame: households in NW Austin
- d) Sample: the 59 houses selected

Just Checking

- Why is each of the following claims not correct?
- It is always better to take a census than to draw a sample

It can be hard to reach all members of a population, and it can take so long that circumstances change, affecting the responses. A well-designed sample is often a better choice.

Just Checking

- Stopping students on their way out of the cafeteria is a good way to sample if we want to know about the quality of the food there.
- The sample is probably biased students who didn't like the food at the cafeteria might choose not to eat there.



Just Checking

- We drew a sample of 100 from the 3000 students in a school. To get the same level of precision for a town of 30,000 residents we will need a sample of 1000
- Only the sample size matters, not the fraction of the overall population.
- A poll taken at a statistic support website garnered 12,357 responses. The majority said they enjoy doing statistics homework. With a sample size that large we can be pretty sure that most statistics students feel this way, too.
- Students who frequent this website might be more enthusiastic about stats than the overall population of stat students. A large sample cannot compensate for this bias.

Just Checking

- The true percentage of all Stats students who enjoy the homework is called the "population statistic"
- It's the population "parameter." "Statistic" describe the samples.

Just Checking

- We need to survey a random sample of 300 of the passengers on a flight from San Francisco to Tokyo. Name each sampling method described:
- 1) Pick every 10th passenger as people board the plane
- Systematic
- 2) From the boarding list randomly sample 5 people flying first class and 25 of the other passengers
- Stratified

Just Checking

- We need to survey a random sample of 300 of the passengers on a flight from San Francisco to Tokyo. Name each sampling method described:
- 3) Randomly generate
 30 seat numbers and
 survey the passengers
 who sit there
- Simple
- 4) Randomly select a seat position (right window, right center, right aisle, etc.)
- Cluster

The Valid Survey

- A valid survey yields the information we are seeking about the population we are interested in:
- Before setting out to survey, ask yourself:
- What do I want to know?Am I asking the right
- respondents?
- Am I asking the right questions?
- What would I do with the answers if I had them; would they address the things I want to know?

Pitfalls to Avoid:

- Know what you want to know!
- Have a clear idea of what you hope to learn and about whom you hope to learn it.
- Use the right frame. Be sure you have an appropriate sampling frame: have you identified the population of interest and sampled from it appropriately?

Pitfalls to Avoid:

• Tune Your Instrument. Be aware of asking questions you do not really need – longer questionnaires yield fewer responses and thus a greater chance of nonresponse bias • Ask specific rather than general questions.

People are not good at estimating their typical behavior:

Better to ask "how many hours of sleep did you get last night" rather than "how much sleep do you usually get?"

Pitfalls to Avoid:

Ask for quantitative results when possible:

How many magazines did you read last week? Rather than

How much do you read: A lot, A moderate amount, A little, None at all • Be careful in phrasing questions:

A respondent may not understand the question or may understand the question differently than the researcher intended it. Respondents may even lie or shade their responses if they feel embarrassed by the question.

Pitfalls to Avoid:

- Subtle differences in phrasing can make a difference:
- "After 9/11, President Bush authorized government wiretaps on some phone calls in the US without getting court warrants, saying this was necessary to reduce the threat of terrorism. Do you approve or disapprove of this?"
- 53% of respondents approved to the first phrasing, but with the second phrasing it was only 46%
 - "After 9/11, George W. Bush authorized government wiretaps on some phone calls in the US without getting court warrants. Do you approve or disapprove of this?"